

# Lingua Project

## (7 bis) Methods

(Sec. 6.6)

The book "**Denotational Engineering**" may be downloaded from:  
<https://moznainaczej.com.pl/what-has-been-done/the-book>

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# An overview of methods

Three categories of methods:

- imperative methods
- object-constructors
- functional methods

concrete methods

abstract methods

met : Method = Procedure | ProSigDen

## procedures

pro : Procedure = ImpPro | FunPro | ObjCon

ipr : ImpPro = ActParDen x ActParDen  $\rightarrow$  Store  $\rightarrow$  Store

fpr : FunPro = ActParDen x TypExpDen  $\rightarrow$  Store  $\rightarrow$  ValueE

oco : ObjCon = ActParDen x Identifier  $\rightarrow$  Store  $\rightarrow$  Store

not in  
AlgDen

## procedure signatures

prs : ProSigDen = ImpProSigDen | FunProSigDen | ObjConSigDen

ips : ImpProSigDen = ForParDen x ForParDen

fps : FunProSigDen = ForParDen x TypExpDen

ocs : ObjConSigDen = ForParDen x Identifier

# Why procedures modify stores? (rather than states?)

if procedures were modifying states  
(an illegal recursion)

Procedure = State → State

State = Env x Sto

Env = ClaEnv x ProEnv x CovRel

ProEnv = Identifier  $\Rightarrow$  Procedure

# Preprocedures

|     |             |                                     |                           |
|-----|-------------|-------------------------------------|---------------------------|
| ppr | : PrePro    | = ImpPrePro   FunPrePro   ObjPreCon | pre-procedures            |
| ipp | : ImpPrePro | = Env $\mapsto$ ImpPro              | imperative pre-procedures |
| fpp | : FunPrePro | = Env $\mapsto$ FunPro              | functional pre-procedures |
| opc | : ObjPreCon | = Env $\mapsto$ ObjCon              | object pre-constructors   |

Preprocedures are necessary to describe  
mutually recursive procedures  
declared in different classes.

When a procedure `pro` is called, we execute the corresponding `pre-pro` in a declaration time environment `dt-env`, i.e., we execute the function

`pre-pro.dt-env : Store  $\rightarrow$  Store`

# Signatures and parameters

|     |             |                            |                              |
|-----|-------------|----------------------------|------------------------------|
| loi | : ListOfIde | = Identifier <sup>c*</sup> | lists of identifiers         |
| dse | : DecSec    | = ListOfIde x TypExpDen    | declaration sections         |
| fpd | : ForParDen | = DecSec <sup>c*</sup>     | formal-parameter-denotations |
| apd | : ActParDen | = ListOfIde                | actual-parameter-denotations |

## constructors

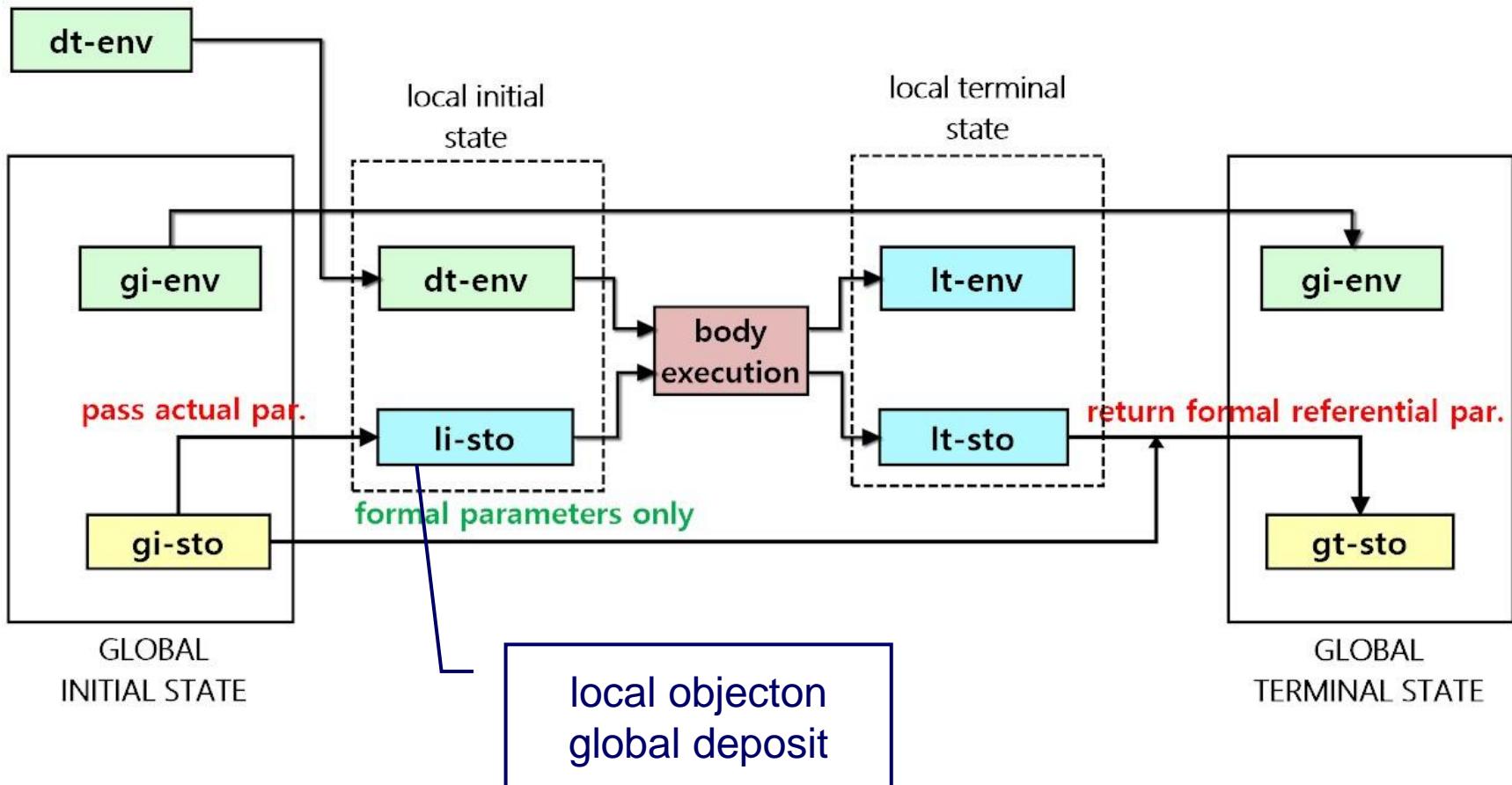
|            |                          |                |                    |
|------------|--------------------------|----------------|--------------------|
| build-loi  | : Identifier             | → ListOfIde    |                    |
| add-to-loi | : Identifier x ListOfIde | → ListOfIde    |                    |
| build-dse  | : ListOfIde x TypExpDen  | → DecSec       |                    |
| build-fpd  | : DecSec                 | → ForParDen    |                    |
| add-to-fpd | : DecSec x ForParDen     | → ForParDen    |                    |
| build-apd  | : ListOfIde              | → ActParDen    | actual-par. denot. |
| build-ipsd | : ForParDen x ForParDen  | → ImpProSigDen | signatures of IP   |
| build-fpsd | : ForParDen x TypExpDen  | → FunProSigDen | signatures of FP   |
| build-ocsd | : ForParDen x Identifier | → ObjConSigDen | signatures of OC   |

value parameters

reference parameters

# The execution of an imperative-procedure call

declaration-time environment



# The creation of an imperative pre-procedure

create-imp-pre-pro : ImpProSigDen x ProDen x Identifier  $\mapsto$  ImpPrePro

create-imp-pre-pro : ForParDen x ForParDen x ProDen x Identifier  $\mapsto$

$\mapsto$  Env  $\mapsto$  ActParDen x ActParDen  $\mapsto$  Store  $\rightarrow$  Store

create-imp-pre-pro.(fpd-v, fpd-r, prd, cl-ide).dt-env.(apd-v, apd-r).ct-sto =

is-error.ct-sto  $\rightarrow$  ct-sto dt- declaration time

**let** ct- call time

li-sto = pass-actual.(fpd-v, fpd-r, apd-v, apd-r, cl-ide).dt-env.ct-sto

is-error.li-sto  $\rightarrow$  ct-sto  $\blacktriangleleft$  error.li-sto

**let** li-sta = (dt-env, li-sto) local initial state

prd.li-sta = ?  $\rightarrow$  ?

**let** lt-sta = prd.li-sta local terminal state

is-error.lt-sta  $\rightarrow$  ct-sto  $\blacktriangleleft$  error.lt-sta

**let** (dt-cle, dt-pre, dt-cov) = dt-env  
(lt-env, lt-sto) = lt-sta  
gt-sto = return-formal.fpd-r.ct-sto.lt-sto.dt-cov

is-error.gt-sto  $\rightarrow$  ct-sto  $\blacktriangleleft$  error.gt-sto

**true**  $\rightarrow$  gt-sto global terminal store

# Siblings and twins of objects

in a context of a common deposit

## INFORMAL DEFINITIONS

A **sibling** of an object:

- the same structure (tree),
- the same names of attributes,
- references differ only with tokens,
- possibly different „leaves” (typed data).

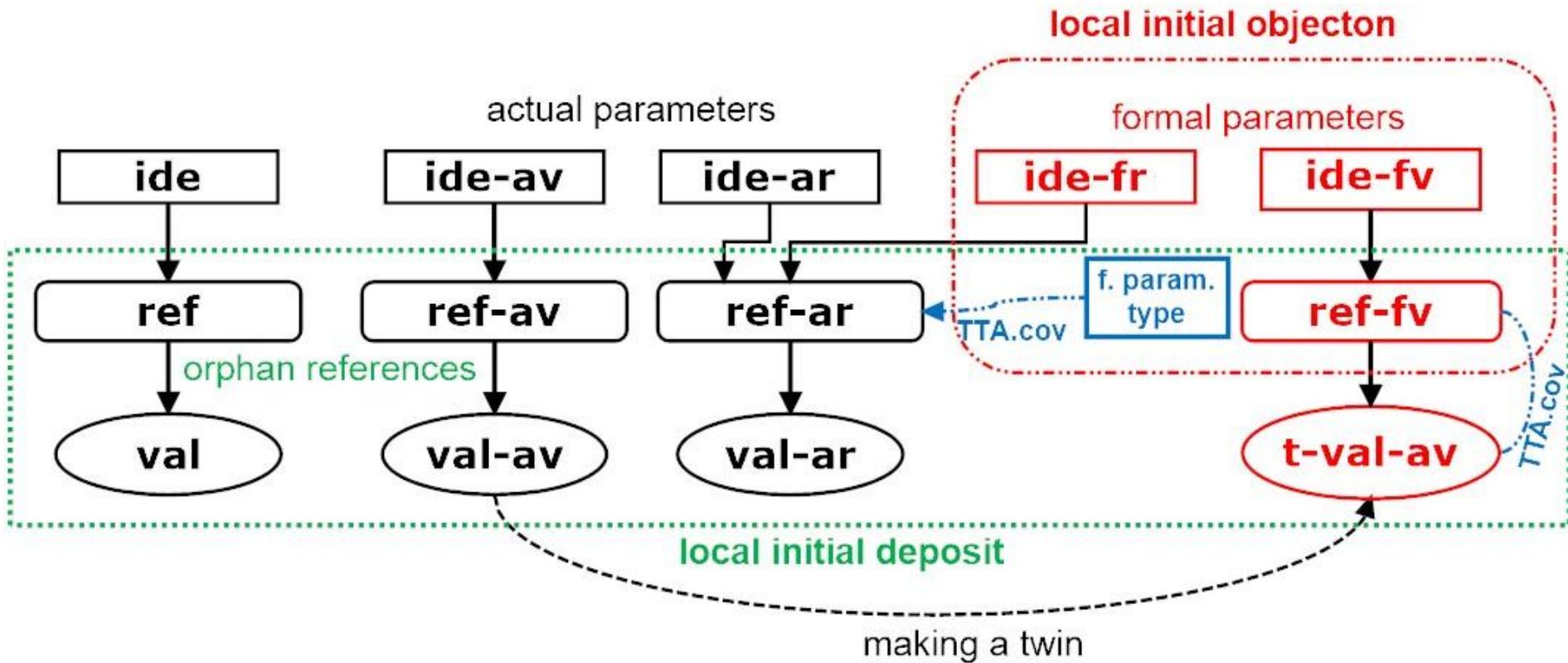
A **twin** of an object:

- a sibling with identical leaves (differ only with references)

Formal definitions in Sec. 4.5

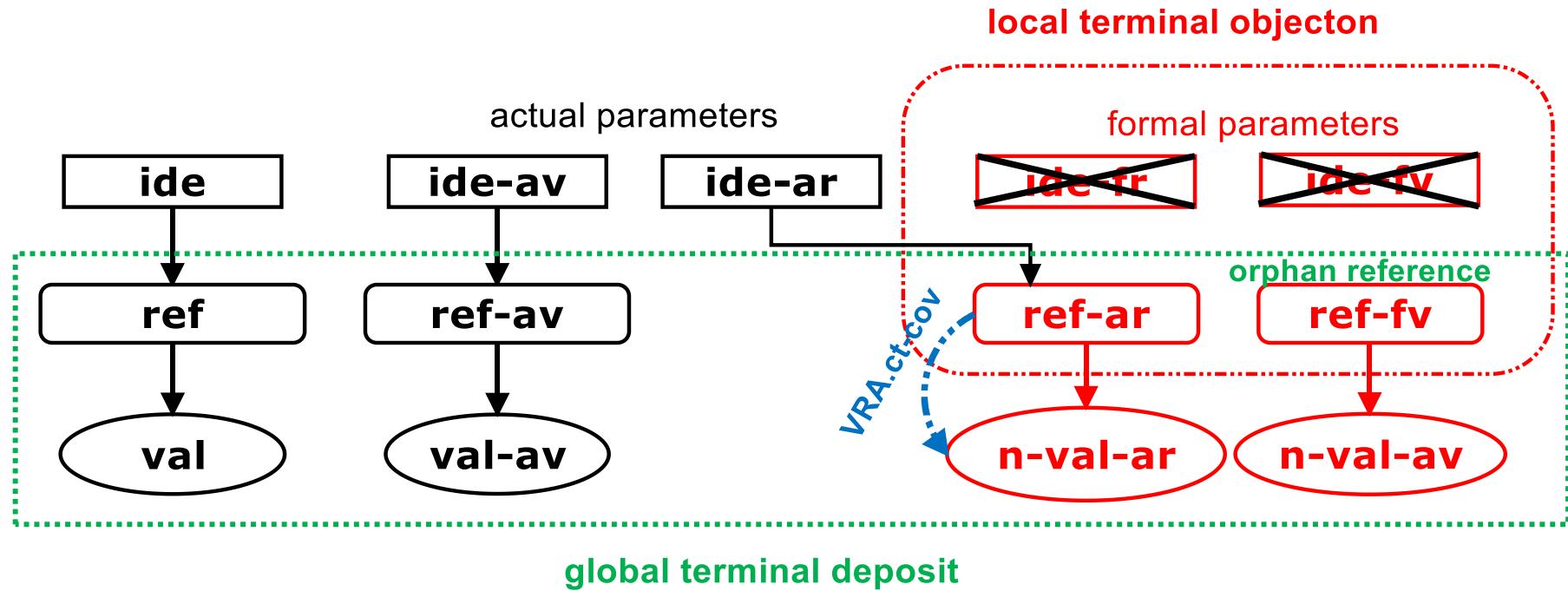
# Passing actual parameters to a procedure

a simplified picture



# Returning references to actual ref. parameters

a simplified picture



## Global terminal state:

- global call-time environment (unchanged)
- global terminal deposit:
  - global call-time objecton; all global variables regain visibility,
  - local terminal deposit; some references become orphans,
  - call-time origin of the store,
  - call-time covering relations (a type checking necessary)

# Calling an imperative procedure

call-imp-pro : Identifier x Identifier x ActParDen x ActParDen  $\mapsto$  InsDen

call-imp-pro : Identifier x Identifier x ActParDen x ActParDen  $\mapsto$

WfState  $\rightarrow$  WfState

call-imp-pro.(cl-ide, pr-ide, apd-v, apd-r).ct-sta =

is-error.ct-sta  $\Rightarrow$  ct-sta

**let**

(ct-env, ct-sto) = ct-sta call-time state

(ct-cle, ct-pre) = ct-env

ct-pre.(cl-ide, pr-ide) = ?  $\Rightarrow$  ct-sta  $\blacktriangleleft$  ‘procedure-unknown’

ct-pre.(cl-ide, pr-ide) /: ImpPro  $\Rightarrow$  ct-sta  $\blacktriangleleft$  ‘imperative-procedure-expected’

**let**

ipr = ct-pre.(cl-ide, pr-ide)

ipr.(apd-v, apd-r).ct-sto = ?  $\Rightarrow$  ?

**let**

gt-sto = ipr.(apd-v, apd-r).ct-sto

**true**  $\Rightarrow$  (ct-env, gt-sto) global terminal store

# The creation of a functional pre-procedure

create-fun-pre-pro : FunProSigDen x ProDen x ValExpDen x Identifier  $\mapsto$   
 $\mapsto$  Env  $\mapsto$  ActParDen  $\mapsto$  Store  $\rightarrow$  ValueE

create-fun-pre-pro.(fps, prd, ved, cl-ide).dt-env.apd.ct-sto =  
is-error.ct-sto  $\rightarrow$  error.ct-sto dt- creation time, ct- call time

let

(ct-obn, ct-dep, ct-sft, ct-ota, 'OK') = ct-sto

(fpd, ted) = fps functional-procedure signature

li-sto = pass-actual.(fpd, (), apd, (), cl-ide ).dt-env.ct-sto local initial store

is-error.li-sto  $\rightarrow$  error.li-sto

let

li-sta = (dt-env, li-sto) local initial state

ex-typ = ted.li-sta the expected type of the returned value

ex-typ : Error  $\rightarrow$  ex-typ

(prd • ved).li-sta= ?  $\rightarrow$  ?

(prd • ved).li-sta : Error  $\rightarrow$  (prd • ved).li-sta

let

(cor, typ) = (prd • ved).sta-li lt- local terminal

not ex-typ TTA.ct-cov typ  $\rightarrow$  'types-incompatible'

true  $\rightarrow$  (cor, ex-typ)

If  $f : A \rightarrow B$  and  $g : B \rightarrow C$  then  $(f \bullet g).a = g.(f.a)$

# Calling a functional procedure

call-fun-pro : Identifier x Identifier x ActParDen  $\rightarrow$  ValExpDen

call-fun-pro : Identifier x Identifier x ActParDen  $\rightarrow$  WfState  $\rightarrow$  ValueE

call-fun-pro.(cl-ide, pr-ide, apd).ct-sta = ct- call time

is-error.ct-sta  $\rightarrow$  ct-sta

**let**

((cle, pre, cov), ct-sto) = ct-sta

pre.(cl-ide, pr-ide) = ?  $\rightarrow$  ‘procedure-unknown’

pre.(cl-ide, pr-ide) /: FunPro  $\rightarrow$  ‘functional-procedure-expected’

**let**

fpr = pre.(cl-ide, pr-ide)

fpr.apd.ct-sto = ?  $\rightarrow$  ?

**true**  $\rightarrow$  fpr.apd.ct-sto

# Object constructors informally

$\text{oco} : \text{ObjCon} = \text{ActParDen} \times \text{Identifier} \rightarrow \text{Store} \rightarrow \text{Store}$

$\text{opc} : \text{ObjPreCon} = \text{Env} \rightarrow \text{ObjCon}$  object preconstructors

$\text{create-obj-pre-con} : \text{ObjConSigDen} \times \text{ProDen} \rightarrow \text{ObjPreCon}$

$\text{create-obj-pre-con} : \text{ForParDen} \times \text{Identifier} \times \text{ProDen} \rightarrow$   
 $\rightarrow \text{Env} \rightarrow \text{ActParDen} \times \text{Identifier} \rightarrow \text{Store} \rightarrow \text{Store}$

The **store-to-store action** of an abject constructor in a class 'MyClass':

1. it creates (obn, 'MyClass') where obn is a twin of the objecton of MyClass
2. it (optionally) modifies current deposit by executing a program; the twin may become a sibling,
3. it creates a reference, assigns it to ide and assigns the sibling to this reference.

# Calling an object constructor

call-obj-con : Identifier x Identifier x Identifier x ActParDen  $\mapsto$  InsDen

call-obj-con : Identifier x Identifier x Identifier x ActParDen

$\mapsto$  WfState  $\rightarrow$  WfState

call-obj-con.(ob-ide, cl-ide, co-ide, apd-v).sta =

is-error.ct-sta  $\Rightarrow$  ct-ct-sta

**let**

((ct-cle, ct-pre), ct-sto) = ct-sta call-time state

ct-pre.(cl-ide, co-ide) = ?  $\Rightarrow$  ct-sta  $\blacktriangleleft$  ‘constructor unknown’

ct-pre.(cl-ide, co-ide) /: ObjCon  $\Rightarrow$  ct-sta  $\blacktriangleleft$  ‘object constructor expected’

**let**

oco = ct-pre.(cl-ide, co-ide)

oco.(apd-v, ob-ide).ct-sto = ?  $\Rightarrow$  ?

**let**

new-sto = oco.(apd-v, ob-ide).ct-sto

**true**  $\Rightarrow$  (ct-env, new-sto)



Thank you for  
your attention